PROLOG

- Widely used in Europe and Japan
- Basis of the 5-th Generation project
- FOL inference system
  - Knowledge base represented using Horn clauses.
    - Program: set of (Horn) clauses.
    - Input data: queries (i.e., FOL sentences to be proved).
    - Output: failure or success + variable bindings.
  - Uses input modus ponens for proofs
    - i.e., depth-first, left-to-right backward chaining.
    - returns on request all the possible solutions.
  - Uses database semantics instead of the general FOL semantics

SYNTAX

- Atoms: constants (including function names and predicate names). Everything not starting with a capital letter or underscore, and everything surrounded by simple quotes is an atom.
- Variables: everything starting with a capital letter or underscore.
- Convenient notation for lists:
  $.(a, b) \rightsquigarrow$ `[A|B]` $.(Joe, .(Jack, .(Jill, [])))) \rightsquigarrow$ `[joe,jack,jill]`.
- Clauses: facts

```
parent(ann,bob).        parent(cecil,dave).
parent(ann,cecil).      parent(cecil,eric).
```

  and rules (with all variables universally quantified).

```
ancestor(A,B) :- parent(A,B).
ancestor(A,C) :- ancestor(A,B), ancestor (B,C).
```

- Queries: FOL sentences (with all variables existentially quantified).

DATABASE SEMANTICS

- Suppose Richard has two brothers, John and Geofrey:

$$Brother(John, Richard) \wedge Brother(Geoffrey, Richard)$$

  - This assertion is always true in a model where Richard has one brother, so we need to add $John \neq Geoffrey$
  - The sentence does not rule out that Richard has more than two brothers
  - The correct assertion therefore is:

$$Brother(John, Richard) \wedge Brother(Geoffrey, Richard) \wedge$$
$$John \neq Geoffrey \wedge$$
$$\forall x \;\; Brother(x, Richard) \Rightarrow (x = John \vee x = Geoffrey)$$

  - Things get complex pretty fast, translating knowledge into knowledge bases becomes exceedingly difficult
- We can use a semantics that provides for more straightforward expressions: database semantics

DATABASE SEMANTICS (CONT'D)

Unique-names assumption: every constant symbol refers to a distinct object

- Breaks down skolemization but makes life easier otherwise

Domain closure: no model contains more domain elements than those named in constant symbols

- Makes model checking feasible (but still very complex)

Closed world assumption: whatever is not known to be true is assumed false

Example

FOL:

$\neg Member(a, [])$
$Member(a, .(a, b))$
$Member(a, c) \Rightarrow$
$\quad Member(a, .(b, c))$

Program (file "`memb.pl`"):

```
memb(A,.(A,B)).
memb(A,.(B,C)) :- memb(A,C).
```

. . . or . . .

```
memb(A,[A|B]).
memb(A,[B|C]) :- memb(A,C).
```

Queries:

```
?- consult(memb).      %% [memb].
Warning: ...some singleton variables...
% memb compiled 0.00 sec, 560 bytes

Yes
?- memb(X,[1,2,3]).

X = 1

Yes
?- memb(X,[1,2,3]).

X = 1 ;

X = 2 ;

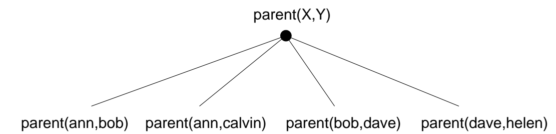
X = 3 ;

No
?-
```


Proof trees

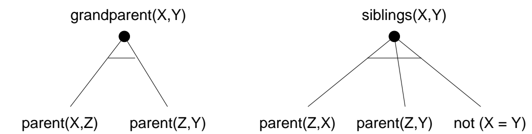
- A family tree:

```
parent(ann,bob).     parent(ann,calvin).
parent(bob,dave).    parent(dave,helen).
```



- Other family relations:

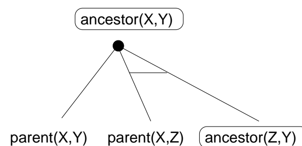
```
grandparent(X,Y) :- parent(X,Z), parent(Z,Y).
siblings(X,Y) :- parent(Z,X),parent(Z,Y), not(X = Y).
```



Proof trees (cont'd)

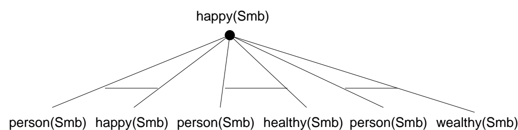
- Yet another family relation:

```
ancestor(X,Y) :- parent(X,Y).
ancestor(X,Y) :- parent(X,Z),ancestor(Z,Y).
```



- A person is happy if she is healthy, wealthy, or wise:

```
happy(Smb) :- person(Smb),happy(Smb).
happy(Smb) :- person(Smb),healthy(Smb).
happy(Smb) :- person(Smb),wise(Smb).
```



Bells and whistles

- Some functions are also defined as infix operators.
  - e.g., `+(1,2)` can be written `1+2`.
- There are some functions and predicates with predefined meaning (e.g., usual relational comparison for numbers).
- Built-in predicate `is` for arithmetic

```
?- X = 1+2.
```

Bells and whistles

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- There are some functions and predicates with predefined meaning (e.g., usual relational comparison for numbers).
- Built-in predicate `is` for arithmetic

```
?- X = 1+2.

X = 1+2 ;

No

?- X is 1+2.

X = 3 ;

No
```


Knights and their tour

```
% Knight jumping on an n x n board.
% The board size is given by the predicate size/1:
size(5).

% The position of the knight is represented by the function pos(X,Y).
% There are 8 possible moves in the middle of the board:
move(pos(I,J), pos(K,L)) :- K = I+1, L = J-2.
move(pos(I,J), pos(K,L)) :- K = I+1, L = J+2.
move(pos(I,J), pos(K,L)) :- K = I+2, L = J+1.
move(pos(I,J), pos(K,L)) :- K = I+2, L = J-1.
move(pos(I,J), pos(K,L)) :- K = I-1, L = J+2.
move(pos(I,J), pos(K,L)) :- K = I-1, L = J-2.
move(pos(I,J), pos(K,L)) :- K = I-2, L = J+1.
move(pos(I,J), pos(K,L)) :- K = I-2, L = J-1.
```


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move(pos(I,J), pos(K,L)) :- K is I+1, L is J+2.
move(pos(I,J), pos(K,L)) :- K is I+2, L is J+1.
move(pos(I,J), pos(K,L)) :- K is I+2, L is J-1.
move(pos(I,J), pos(K,L)) :- K is I-1, L is J+2.
move(pos(I,J), pos(K,L)) :- K is I-1, L is J-2.
move(pos(I,J), pos(K,L)) :- K is I-2, L is J+1.
move(pos(I,J), pos(K,L)) :- K is I-2, L is J-1.

% However, if the knight is somwhere close to board's margins, some
% moves might fall out of the board:
inside(pos(A,B)) :- size(Max), A > 0, A =< Max, B > 0, B =< Max.

search1(A,A,[]).
search1(A,B,[X|Moves]) :- move(A,X), inside(X), search1(X,B,Moves).
```


Knights and their tour (cont'd)

```
?- [knights].
% knights compiled 0.00 sec, 336 bytes

Yes
?- search1(pos(0,0),pos(1,2),M).

M = [pos(1, 2)]
```

Knights and their tour (cont'd)

```
?- [knights].
% knights compiled 0.00 sec, 336 bytes

Yes
?- search1(pos(0,0),pos(1,2),M).

M = [pos(1, 2)] ;

ERROR: Out of local stack
   Exception: (16,218) move(pos(5, 2), _G116577) ? abort
% Execution Aborted
?-
```


Knights and their tour (cont'd)

```
search(A,B,R) :- search_aux(A,B,[A],R).

search_aux(Z,Z,L,R) :- reverse(L,R).
search_aux(X,Y,L,R) :- move(X,Z), inside(Z),
                       not(member(Z,L)),     % ISO: \+ member(Z,L)
                       search_aux(Z,Y,[Z|L],R).
```

. . . and then:

```
?- search(pos(0,0),pos(1,2),M).

M = [pos(0, 0), pos(1, 2)] ;

M = [pos(0, 0), pos(2, 1), pos(3, 3), pos(4, 1), pos(2, 2) |...] ;

M = [pos(0, 0), pos(2, 1), pos(3, 3), pos(4, 1), pos(2, 2), |...] ;
```

. . . and so on (about 127 solutions!).

CSP

Map colouring.

```
% problem instance
border(a,b).    border(a,c).    border(d,e).    border(b,e).
border(a,d).    border(b,c).    border(e,c).    border(d,c).

adj(X,Y) :- border(X,Y).
adj(X,Y) :- border(Y,X).

colour(X) :- member(X,[red,green,blue]).

colour_map([],Colouring,Colouring).
colour_map([Country|Countries], Colouring, R) :-
    colour(X), \+ conflict(Country,X,Colouring),
    colour_map(Countries,[colour(X,Country)|Colouring],R).

% violates constraint?
conflict(Country,X,Colouring) :-
    adj(Country,Country1),  % more efficient if we call adj/2 first
    member(colour(X,Country1),Colouring).
```


Negation as failure

- Negation in Prolog: `not/1` or `\+/1`.
- Recall that Prolog assumes the closed world paradigm. The negation is therefore different from logical negation:

```
?- member(X,[1,2,3]).
X = 1 ;
X = 2 ;
X = 3 ;
No

?- not(member(X,[1,2,3])).
No

?- not(not(member(X,[1,2,3]))).
X = _G332 ;
No
```

  - `not/1` fails upon resatisfaction (a goal can fail in only one way).
  - `not/1` does not bind variables.

Negation in case selections

```
positive(X) :- X > 0.
negative(X) :- X < 0.

sign(X,+) :- positive(X).
sign(X,-) :- negative(X).
sign(X,0).
```

```
?- sign(1,X).
```


Negation in case selections


```
positive(X) :- X > 0.
negative(X) :- X < 0.

sign(X,+) :- positive(X).
sign(X,-) :- negative(X).
sign(X,0).
```



```
?- sign(1,X).

X = + ;

X = 0 ;

No
```


Negation in case selections


```
positive(X) :- X > 0.
negative(X) :- X < 0.

sign(X,+) :- positive(X).
sign(X,-) :- negative(X).
sign(X,0).
```

```
?- sign(1,X).

X = + ;

X = 0 ;

No
```



```
sign1(X,+) :- positive(X).
sign1(X,-) :- negative(X).
sign1(X,0) :- not(positive(X)),
              not(negative(X)).
```

```
?- sign1(1,X).

X = + ;

No
```


Modifying the search space

The `!/0` predicate (pronounced “cut”) does not allow backtracking over it. All attempts to redo goals to the left of the cut fail.

Commit:

```
negative(X) :- X < 0.

sign(X,-) :- negative(X).
sign(X,+).

even(X) :- R is X rem 2, R = 0.

positive_even1(X) :- sign(X,+), even(X).
positive_even(X) :- sign(X,+), !, even(X).

?- positive_even1(-4).

Yes
?- positive_even(-4).

No
```

Succeed once:

```
member(X,[X,_]).
member(X,[_,Y]) :- member(X,Y).

membchk(X,[X,_]) :- !.
membchk(X,[_,Y]) :- membchk(X,Y).
```

MODIFYING THE SEARCH SPACE (CONT'D)

- Succeed once (cont'd):

```
fact1(1,1).                   fact2(1,1).
fact1(N,R) :- N1 is N-1,      fact2(N,R) :- N>1, N1 is N-1,
              fact1(N1,R1),                 fact2(N1,R1), R is N*R1.
              R is N*R1.
                              fact3(1,1) :- !.
                              fact3(N,R) :- N1 is N-1,
                                            fact3(N1,R1), R is N*R1.
```

- Fail goal now
  - An apparently useless predicate: `fail/0` always fails.

```
not(P) :- P, !, fail.                  not(P).
```


MODIFYING THE SEARCH SPACE (CONT'D)

- Succeed once (cont'd):

```
fact1(1,1).                   fact2(1,1).
fact1(N,R) :- N1 is N-1,      fact2(N,R) :- N>1, N1 is N-1,
              fact1(N1,R1),                 fact2(N1,R1), R is N*R1.
              R is N*R1.
                              fact3(1,1) :- !.
                              fact3(N,R) :- N1 is N-1,
                                            fact3(N1,R1), R is N*R1.
```

- Fail goal now
  - An apparently useless predicate: `fail/0` always fails.

```
not(P) :- P, !, fail.                  not(P).
```


  - Another useful predicate: `call/1`.
    * `call(P)` behaves as if `P` were passed as a goal to the interpreter.

```
not(P) :- call(P), !, fail.                  not(P).
```


AN ADVENTURE GAME

- Consider the following knowledge base:

```
location(egg,duck_pen).
location(ducks,duck_pen).
location(fox,woods).
location(you,house).

connect(yard,house).
connect(yard,woods).

is_closed(gate).
connect(duck_pen,yard) :- is_open(gate).
```

- We want to move around, be able to open and close the gate, pick the egg, and so on.

- In order to do this we need to modify the knowledge base dynamically.

MODIFYING THE KNOWLEDGE BASE

- Adding a fact to the knowledge base:
  - `assert` adds the fact given as argument somewere
  - `asserta` adds the fact given as argument at the beginning of the knowledge base
  - `assertz` adds the fact given as argument at the end
  - all variants succeed only once

- Removing a fact from the knowledge base:
  - `retract` removes one instance that unifies with the argument
  - removes one more instance at each redo attempt
  - fails when no removal is possible

CONVINCING THE KNOWLEDGE BASE TO ALLOW CHANGES

- All the industrial grade PROLOG implementations compile the knowledge base as to increase the speed of retrieving facts from it.
  - SWI PROLOG is one such an example
- In these variants, you need to specify which facts are changeable at run time.
  - These predicates will be stored separately, in an un-optimized fashion
  - The `dynamic` declaration must precede the predicate definition

```
:-  dynamic(you_have/1),
    dynamic(location/2),
    dynamic(is_closed/1),
    dynamic(is_open/1).
```


ADVENTURE GAME (CONT'D)

- Moving around:

```
goto(X) :-
       location(you,L),
       (connect(L,X); connect(X,L)),
       retract(location(you,L)),
       assert(location(you,X)),
       write(' You are in the '),
       write(X), nl.
goto(X) :- write(' You cannot get there '), nl.
```

- Picking up the egg:

```
pick(egg) :-
           location(you,duck_pen),
           not you_have(egg),
           assert(you_have(egg)),
           write(' You picked the egg '), nl.
pick(X) :- write(' There is nothing to pick '), nl.
```


ADVENTURE GAME (CONT'D)

- Opening the gate:

```
open(gate) :-
            location(you,yard),
            is_closed(gate),
            retract(is_closed(gate)),
            assert(is_open(gate)),
            write(' Opened. '), nl.
open(X) :- write(' You cannot open that '), nl.
```

- How the other creatures react:

```
ducks :-
       is_opened(gate),
       retract(location(ducks,duck_pen)),
       assert(location(ducks,yard)).
ducks.

fox :-
     location(ducks,yard),
     location(you,house),
     write(' The fox has taken a duck '), nl.
fox.
```


ADVENTURE GAME (CONT'D)

- The main loop:

```
go :- done.
go :-
    write('>>'),
    read(X),
    call(X),
    go.

done :-
      location(you,house),
      you_have(egg),
      ducks, fox,
      write(' Thanks for getting the egg. '), nl.
```

SAMPLE INTERACTION

```
?- go.
>>goto(yard).
 You are in the yard
>>goto(duck_pen).
 You cannot get there from here
>>pick(egg).
 There is nothing to pick
>>open(gate).
 Opened.
>>goto(duck_pen).
 You are in the duck_pen
>>pick(egg).
 You picked the egg
>>goto(house).
 You cannot get there from here
>>goto(yard).
 You are in the yard
>>goto(house).
 You are in the house
 The fox has taken a duck
 Thanks for getting the egg.
yes
```