

# Introduction to Software Specifications

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- Coordinates:
  - **Course Web page:** <http://cs.ubishops.ca/home/cs310>
  - Instructor: Stefan Bruda  
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  - **Office hours?**
- Textbook (required): **R. D. Tennent, Specifying Software: A Hands-On Introduction, Cambridge University Press, 2002**
  
- Two subjects:
  - Formal languages
  - Program specification and reasoning about program correctness



- Describe **problems** in a formal way so that we can reason about them (**syntax**)
- Describe how a problem can be solved computationally (**semantics**)
- Example of the impact of theory to practice
  - Lexical and parsing stages of compiler construction
  - Use of regular expressions in text editors
  - State-charts in object-oriented modeling
  - Circuit design
  - DNA and protein sequence matching
  - Behaviour of reactive systems
- Also useful in answering fundamental questions such as whether **there exist tasks/problems that cannot be solved algorithmically** and, if yes, which tasks are algorithmically solvable and which are not



# FORMAL LANGUAGES (CONT'D)

- Formal languages = the mathematics of strings of symbols
- **Alphabet** = a finite, nonempty set of elements (symbols, tokens, characters)
- **String** (word) over an alphabet  $\Sigma$  = finite sequence of symbols of  $\Sigma$  (a string in  $\Sigma^*$ )
  - $\varepsilon$  = the **empty string**
  - Examples: cat, dog, mouse, Fluffy, xzrbstuph, 0011011100, -36.557
- **Language** over  $\Sigma$  = set of strings over  $\Sigma$ 
  - Examples:
    - The English language
    - $\{w : w \text{ is the name of a cat}\}$
    - $\{n \in \{0, 1\}^* : \exists x, y, z \in \mathbb{N} : x^n + y^n = z^n\}$
    - $\{g \in (\mathbb{N} \times \mathbb{N})^* : \text{the graph } g \text{ has a Hamiltonian path}\}$
  - **Finite** (or not), **finite representation** (or not), **mathematical representation**
  - We want to analyze how problems are solved computationally, so we study **formal** (systematic, computational) **descriptions**



- A program transforms input values to output values in a particular way, so a specification describes transformations from input values to output values
- Therefore a specification consists in the following parts:
  - What the **input** will be
  - What the **output** should be
  - What is the **environment** in which the specification/program should work
- Input and output refer to things that can be **observed**: input and output variables and constraints on the variables
- The formalization of a specification consists in the following:
  - **Declarative interface**: static properties of the identifiers
  - **Pre-conditions**: assertion on input values that the program will be given
  - **Post-condition**: assertion on output values, possibly in relation to input values



- **A specification is a contract:** the software designer agrees to establish the post-condition if the program is started in a way that satisfies the pre-condition
  - If the program is run in a context not covered by the pre-condition, it can run in any way without “breaking” the contract
- In this course we will develop logic-based techniques to verify correctness of small programs (algorithms)
  - That is, the goal is to prove that a program does what a specification says it should do
  - We use logical formulas (assertions) as comments in programs
    - We **assert** that the formula should be true when flow of control reaches it
- Such techniques are generally too time consuming to be used directly with large software systems
  - In these cases **formal methods** are used instead
  - Combination of **program specification** and **formal languages**!